ELECTRON ENERGY SPECTRUM AND MAGNETIC INTERACTIONS

IN HIGH-T$_C$ SUPERCONDUCTORS

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The character of magnetic interactions in La-Sr-Cu-O and Y-Ba-Cu-O systems is of primary importance for analysis of high-T$_C$ superconductivity in these compounds. Neutron diffraction experiments showed the antiferromagnetic ground state for nonsuperconducting La_2CuO_4 and $YBa_2Cu_3O_6$ with the strongest antiferromagnetic superexchange being in the ab plane [1,2]. Nonsuperconducting "1-2-3" system has even two Neel temperatures T_{N1} and T_{N2}. The first one corresponds to the ordering of Cu atoms in the CuO_2 planes, T_{N2} reflects the antiferromagnetic ordering of magnetic moments in CuO chains relatively to the moments in the planes T_{N1} and T_{N2} depend strongly on the oxygen content [3] (T_{N1}=450 K for X=0,1 and T_{N2}=80 K, but T_{N1}=230 K and T_{N2}=10 K for X=0.35).

We have tried to describe magnetic interactions in high-T superconductors basing on the LMTO band structure calculations. Exchange interaction parameters can be defined from the effective Heisenberg hamiltonian:

$$H_{ex} = -1/2 \sum_{ij} J_{ij} \vec{S}_i \vec{S}_j \tag{1}$$

When the magnetic moments are not too large, as copper magnetic moments in superconducting oxides, J_{ij} parameters can be defined through the non-local magnetic susceptibility of spin-restricted solution for the crystal [4,5]:

$$J_{ij} = \frac{1}{2} \frac{I_i \cdot I_j}{S_i \cdot S_j} \sum_{LL'} \chi_{LL'}^{ij} \tag{2}$$

where

$$\chi_{LL'}^{ij} = 1/\pi \int^{E_F} Im \, G_{LL'}^{ij}(E) \cdot G_{L'L}^{ji}(E) \, dE \quad , \tag{3}$$

$$G_{LL'}^{ij} = 1/\Omega_{BZ} \int_{BZ} d\vec{k} \sum_n \frac{\psi_{nl}(\vec{k}) \psi_{nl}^*(\vec{k})}{E - E_n(\vec{k})} e^{i\vec{k} \cdot \vec{R}_{ij}} \tag{4}$$

- is the nondiagonal Green function which can be calculated through the energy spectrum $E_n(\vec{k})$ and $\psi_{nl}(\vec{k})$ of the LMTO-hamiltonian. I_l in formulae (2) is interatomic exchange parameters of atom i. Due to the sharp dependence of nondiagonal Green function $G_{LL}^{ij}(E)$ on the E the integral (3) should be calculated as contour integral in complex plane.

The results of nonlocal magnetic susceptibility calculations and the values of exchange interaction parameters for La CuO and $YBa_2Cu_3O_7$ systems are given in the Table.

Strong anisotropy of exchange interactions in the ab plane and along the c axis in La_2CuO_4 is obviously seen. The value of Neel temperature found agrees well with the experimental data available. In the $YBa_2Cu_3O_7$ system there is strong antiferromagnetic Cu-O-Cu interaction in the CuO_2 plane, which results in antiferromagnetic ground state of $YBa_2Cu_3O_6$.

Superexchange of Cu1-O4-Cu2 type is antiferromagnetic also, in accordance with the experiment. Using the simplest mean field approximation $T_N = \frac{1}{3}|J|zS(S+1)$, where z is the number of the nearest magnetic neighbours, it is possible to estimate Neel temperature values. They are T_{N1} = 265-314 K, T_{N2} = 61 K agree well with the experimental data. Large ferromagnetic moment exchange in Cu1-O4-Cu1 chains (which follows from NMR experiments [6] also) does not influence antiferromagnetic ordering, as when δ = 1 all the chaines are broken.

In the planes of "1-2-3"system there are quite strong antiferromagnetic Cu-O and O-O interaction which appear due to holes in oxigen subbands. These results are in line with the magnetic model of oxigen holes pairing in high-T_c superconductors suggested in [7].

We have performed also a number of LMTO spin-polarised calculations for $GdBa_2Cu_3O_6$ and $GdBa_2Cu_3O_7$ both for ferromagnetic and antiferromagnetic ordering of magnetic moments. For antiferromagnetic state the energy gap of 0,04 ev is formed at the Fermi level. Spin splitting of Gd f-states equals to 5 ev, and magnetic moment of Gd atoms is 7.3 μ_B. The estimation of stability parameters [8] leads to the conclusion of more stable antiferromagnetic ordering: the difference of J_0 parameters is 230 K (O_6) and 180 K (O_7). The value of s-f integral in antiferromagnetic phase of $GdBa_2Cu_3O_7$ appears to be about 20 K, and correspond to small changes of T_c when Gd atoms enter the crystal lattice.

Table. Exchange interaction parameters for $YBa_2Cu_3O_7$ and La_2CuO_4 (for s=1/2 and $I_{Cu}=0,07$ Ry, $I_O=0,11$ Ry)

pair	$\hat{R}_{ij}$	$\chi^{ij}_{dd(p)}$ (mRy^{-1})	J^{ij} (K)
$YBa_2Cu_3O_7$			
Cu2-O2-Cu2	(0 1 0)	-50,8	-157
Cu2-O3-Cu2	(1 0 0)	-42,8	-132
Cu1-O4-Cu2	(0 0 1)	-9,9	-31
Cu1-O1-Cu1	(0 1 0)	72,5	225
Cu2-O2	(0,5 0 0)	112,3	545
O2-O2	(0,5 0,5 0)	35,5	270
La_2CuO_4			
Cu-O1-Cu	(1 0 0)	-73,5	227
Cu-O2-Cu	(0 0 1)	-0,45	1,4

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